

$$x^2 + y^2 - 2x - 4y - 4 = 0 \quad \left(\frac{b}{2}\right)^2$$

$$(x^2 - 2x + 1) + (y^2 - 4y + 4) = 4$$

write in standard form

$$(x-1)^2 + (y-2)^2 = 9$$

$$C: (1, 2)$$

$$r: 3$$

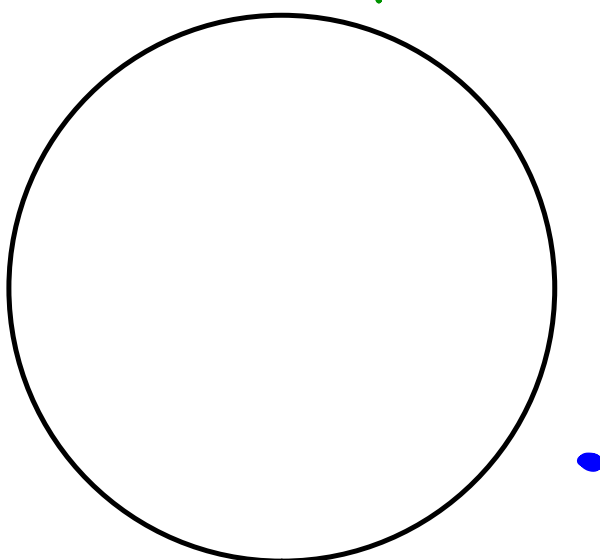
Check in: 2:05

Check out: 3:25

On
— = r^2
 $q = q$

In
 $< r^2$

Out
 $> r^2$



Location of Points and Their Equations

On the Circle Inside the Circle Outside the Circle

Determining if a Point is on the Circle

Standard Form of Circles

$$(x - h)^2 + (y - k)^2 = r^2$$

Given a circle, you can verify whether a point lies on the circle by:

*substituting the coordinates of the point into the equation to see if the resulting equation is true

1. A circle has a radius of 2 and a center of (2, -3). Will the following points lie on the circle?

Equation of Circle: $(x-2)^2 + (y+3)^2 = 4$

a. (2, -5)

Substitute point into equation to see if resulting equation is true.

$$\begin{aligned} (2-2)^2 + (-5+3)^2 &= 4 \\ 0^2 + (-2)^2 &= 4 \\ 0 + 4 &= 4 \end{aligned}$$

$$4 = 4 \quad \text{on the circle}$$

Conclusion: _____

b. (3, -1)
x y

$$(x-2)^2 + (y+3)^2 = 4$$

Substitute point into equation to see if resulting equation is true.

$$(3-2)^2 + (-1+3)^2 = 4$$

$$(1)^2 + (2)^2 = 4$$

$$1 + 4 = 4$$

Conclusion: _____

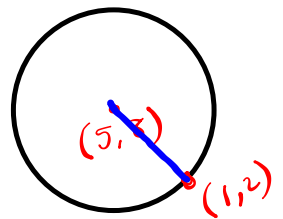
$$5 > 4$$

outside
the circle

Flip onto back

ex. 2

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$



center is $(5, 8)$ with a point on the circle at $(1, 2)$

find the radius and determine where the point $(3, 2)$ is.

$$r = \sqrt{(1-5)^2 + (2-8)^2}$$

$$\sqrt{(-4)^2 + (-6)^2}$$

$$\sqrt{16 + 36} = \sqrt{52}$$

$$(x-h)^2 + (y-k)^2 = r^2$$

$$(x-5)^2 + (y-8)^2 = 52$$

$$(3-5)^2 + (2-8)^2 = 52$$

$$(-2)^2 + (-6)^2 = 52$$

$$4 + 36 = 52$$

$$40 < 52$$

inside
the
circle