

$$y - y_1 = m(x - x_1)$$

2) through: $(-1, -2)$, parallel to $y = 3x - 2$

$$m = 3$$

$$y + 2 = 3(x + 1)$$

$$y + 2 = 3x + 3$$

$$y = 3x + 1$$

3) through: $(1, 3)$, perp. to $y = -\frac{1}{4}x + 2$

$$m = -\frac{1}{4} \rightarrow m = 4$$

$$y - 3 = 4(x - 1)$$

$$y - 3 = 4x - 4$$

$$y = 4x - 1$$

4) through: $(-1, 0)$, perp. to $y = x$

$$m = 1 \rightarrow m = -1$$

$$y - 0 = -1(x + 1)$$

$$y = -x - 1$$

Find the distance between each pair of points.

5) $(-2, 8), (-7, -8)$

$$\sqrt{25 + 256}$$
$$\sqrt{281}$$
$$16.76$$

6) $(1, -5), (-5, 3)$

$$\sqrt{36 + 64}$$
$$\sqrt{100}$$
$$10$$

Find the midpoint of the line segment with the given endpoints.

7) $(1, 1), (-5, 0)$

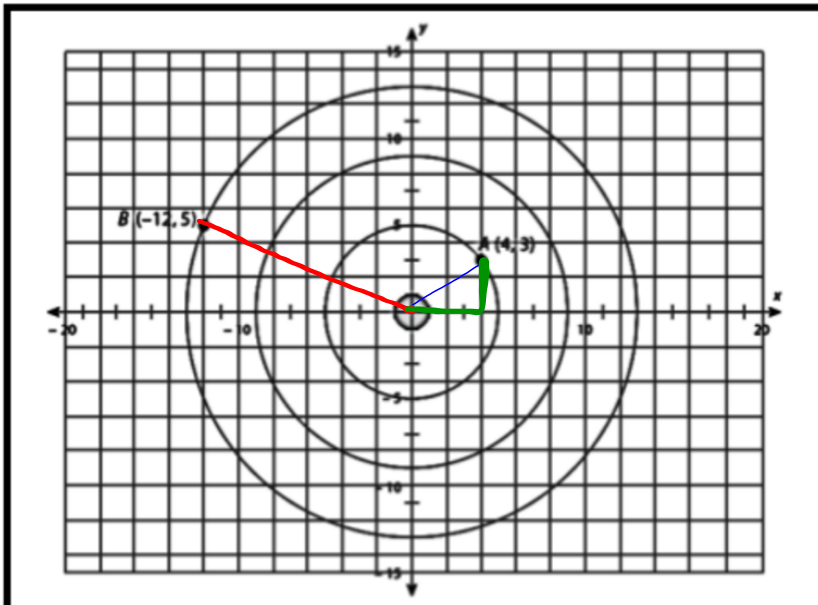
$$\left(\frac{1 + -5}{2}, \frac{1 + 0}{2} \right)$$
$$(-2, \frac{1}{2})$$

8) $(10, 0), (3, -7)$

$$\left(\frac{10 + 3}{2}, \frac{0 + -7}{2} \right)$$
$$(6.5, -3.5)$$

Equations of Circles and Their Graphs

A video game designer created the following diagram of a target.



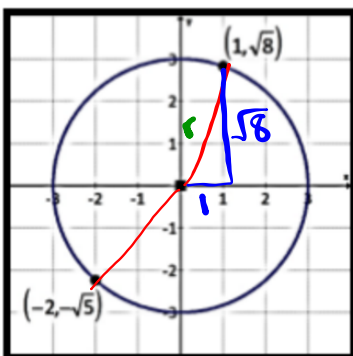
What is the radius from the center to point A? $(4, 3)$ $(0, 0)$

$$\begin{aligned} &\sqrt{(4-0)^2 + (3-0)^2} \\ &\sqrt{16 + 9} \\ &r = \sqrt{25} \\ &r = 5 \end{aligned}$$

What is the radius from the center to point B? $(-12, 5)$ $(0, 0)$

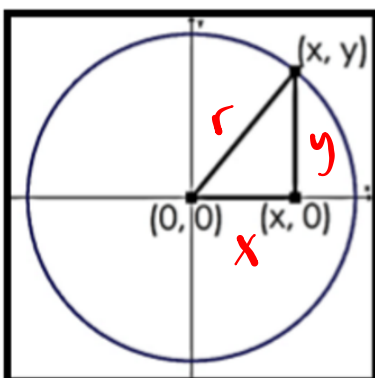
$$\begin{aligned} &\sqrt{(0+12)^2 + (0-5)^2} \\ &\sqrt{144 + 25} \\ &r = \sqrt{169} = 13 \end{aligned}$$

Deriving the Equation of a Circle



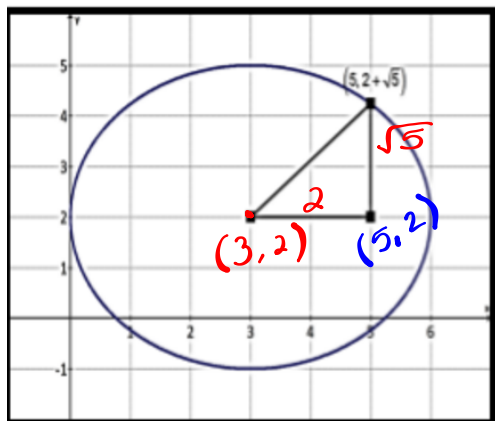
Using the Pythagorean Theorem, prove the radius of the circle is a length of 3 units using the given points.

$$\begin{aligned} 1^2 + (\sqrt{8})^2 &= r^2 \\ 1 + 8 &= r^2 \\ 9 &= r^2 \\ \boxed{r = 3} \end{aligned}$$



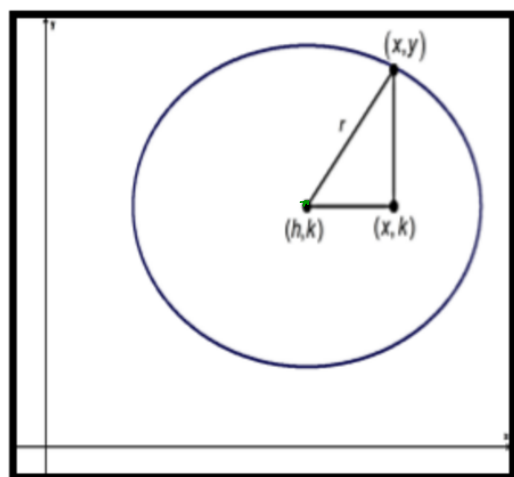
An arbitrary point has been placed on a general circle with radius r . Label the right triangle's legs and hypotenuse and write the Pythagorean Theorem equation that models your triangle.

$$x^2 + y^2 = r^2$$



Using the Pythagorean Theorem, prove the radius of the circle is a length of 3 units using the given point.

$$\begin{aligned}
 (5-3)^2 + (2+\sqrt{5}-2)^2 &= r^2 \\
 2^2 + (\sqrt{5})^2 &= r^2 \\
 4 + 5 &= r^2 \\
 9 &= r^2 \\
 r &= 3
 \end{aligned}$$



Arbitrary points have been placed on a general circle with radius r . Label the right triangle's legs and hypotenuse and write the Pythagorean Theorem equation that models your triangle.

$$\boxed{(x-h)^2 + (y-k)^2 = r^2}$$

$C: (h, k)$

Equations of Circles

A circle is the set of all points (x, y) in a plane that are equidistant from a fixed point called the center of the circle. The distance between the center and any point (x, y) on the circle is called the radius.

The Standard Form of a Circle

Centered at the Origin: $(0,0)$

$$x^2 + y^2 = r^2$$

$(0,0)$ is the center

r is the radius

The Standard Form of a Circle

Centered Not at the Origin:

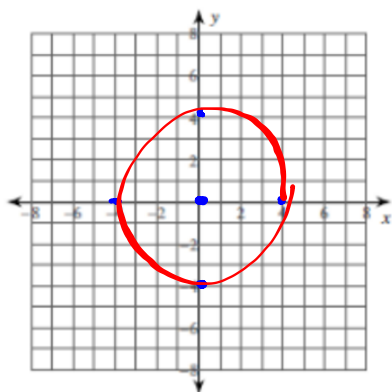
$$(x - h)^2 + (y - k)^2 = r^2$$

(h, k) is the center

r is the radius

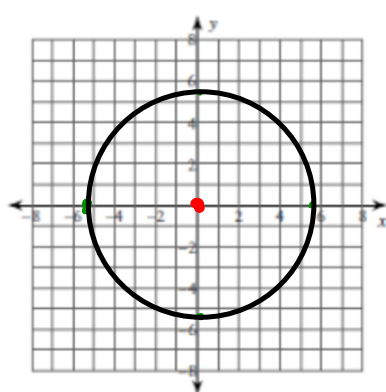
a. $x^2 + y^2 = 16$

C: $(0, 0)$ r: $\sqrt{16} = 4$



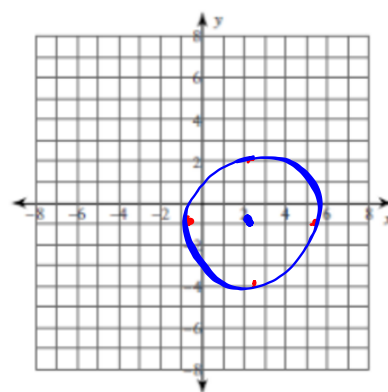
b. $x^2 + y^2 = 30$
 $x^2 + y^2 = r^2$

C: $(0, 0)$ r: $\sqrt{30} = 5.4$



c. $(x - 2)^2 + (y + 1)^2 = 9$

C: $(2, -1)$ r: $\sqrt{9} = 3$



Writing Equations of Circles Given Graphs

Write the center, radius, and equation of the circle.

1. C = $(1, -3)$

r = 2

Eqtn: $(x - 1)^2 + (y + 3)^2 = 4$

2. C = $(2, -1)$

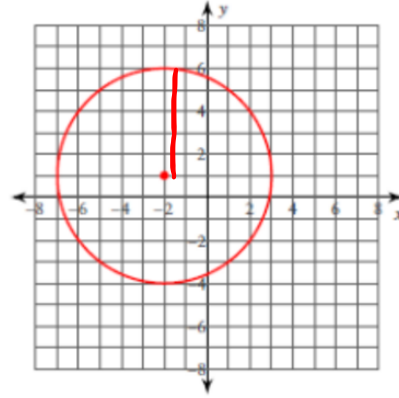
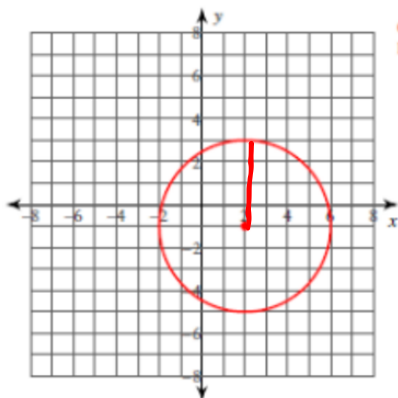
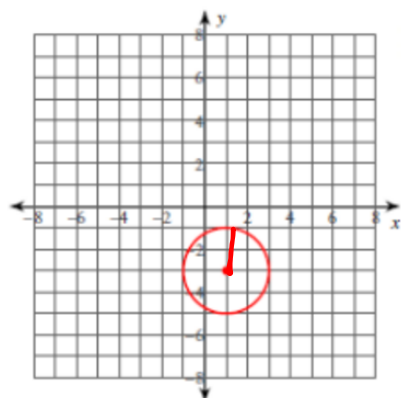
r = 4

Eqtn: $(x - 2)^2 + (y + 1)^2 = 16$

3. C = $(-2, 1)$

r = 5

Eqtn: $(x + 2)^2 + (y - 1)^2 = 25$



 Writing Equations of Circles

 1. Write the equation of a circle with the given **radius** and whose **center is the origin**.
a. $r = 11$

$$x^2 + y^2 = 121$$

b. $r = \sqrt{17}$

$$x^2 + y^2 = 17$$

c. $2\sqrt{5}$

$$x^2 + y^2 = 20$$

$$(2\sqrt{5})^2 = 4 \cdot 5 = 20$$

 2. Write the equation of a circle with the given **radius and center**.
a. Center at $(-2, 3)$ and radius of 4

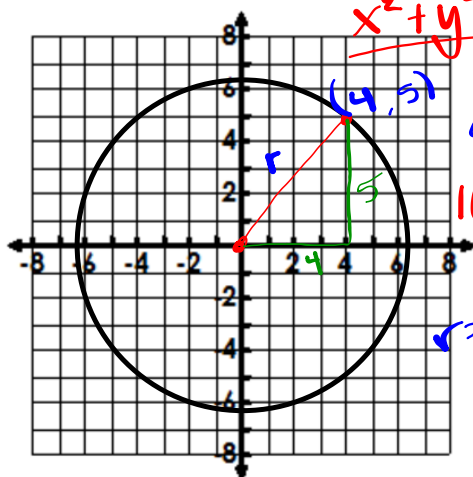
$$(x+2)^2 + (y-3)^2 = 16$$

b. Center at $(0, -5)$ and radius of $3\sqrt{10}$

$$x^2 + (y+5)^2 = 90$$

 3. Write the equation given a **point on the circle and its center**.

$r =$

a. Point $(4, 5)$ and Center $(0, 0)$ 

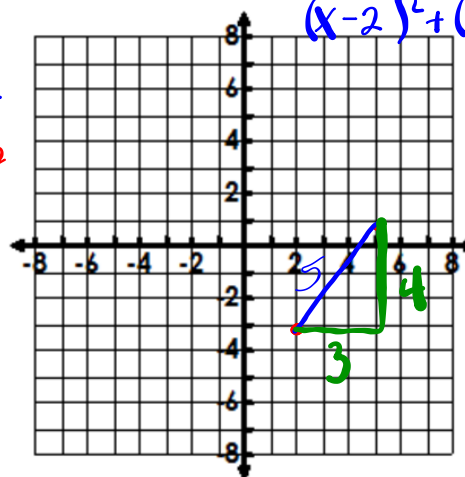
$$x^2 + y^2 = 41$$

$$4^2 + 5^2 = r^2$$

$$16 + 25 = r^2$$

$$41 = r^2$$

$$r = \sqrt{41}$$

b. Point at $(5, 1)$ and Center at $(2, -3)$ 

$$(x-2)^2 + (y+3)^2 = 25$$

$$3^2 + 4^2 = r^2$$

$$9 + 16 = r^2$$

$$25 = r^2$$

$$r = 5$$

c. Point $(0, 2)$ and Center at $(-6, 3)$ d. Point $(2, 5)$ and Center $(0, 0)$